

F.Sc Math Part 1

Trigonometric Values Handout

Trigonometric Values Handout and Review Notes

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Study Notes

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Guess Papers

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Schemes



مزید نوٹس، گزشتہ پیپرز، ٹیسٹ پیپرز، گیس پیپرز، ڈیٹ شیٹ، رزلٹ اور بہت کچھ۔

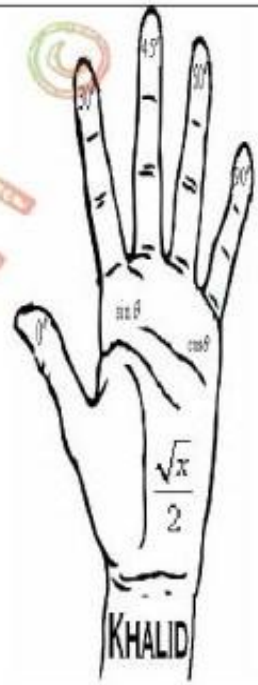
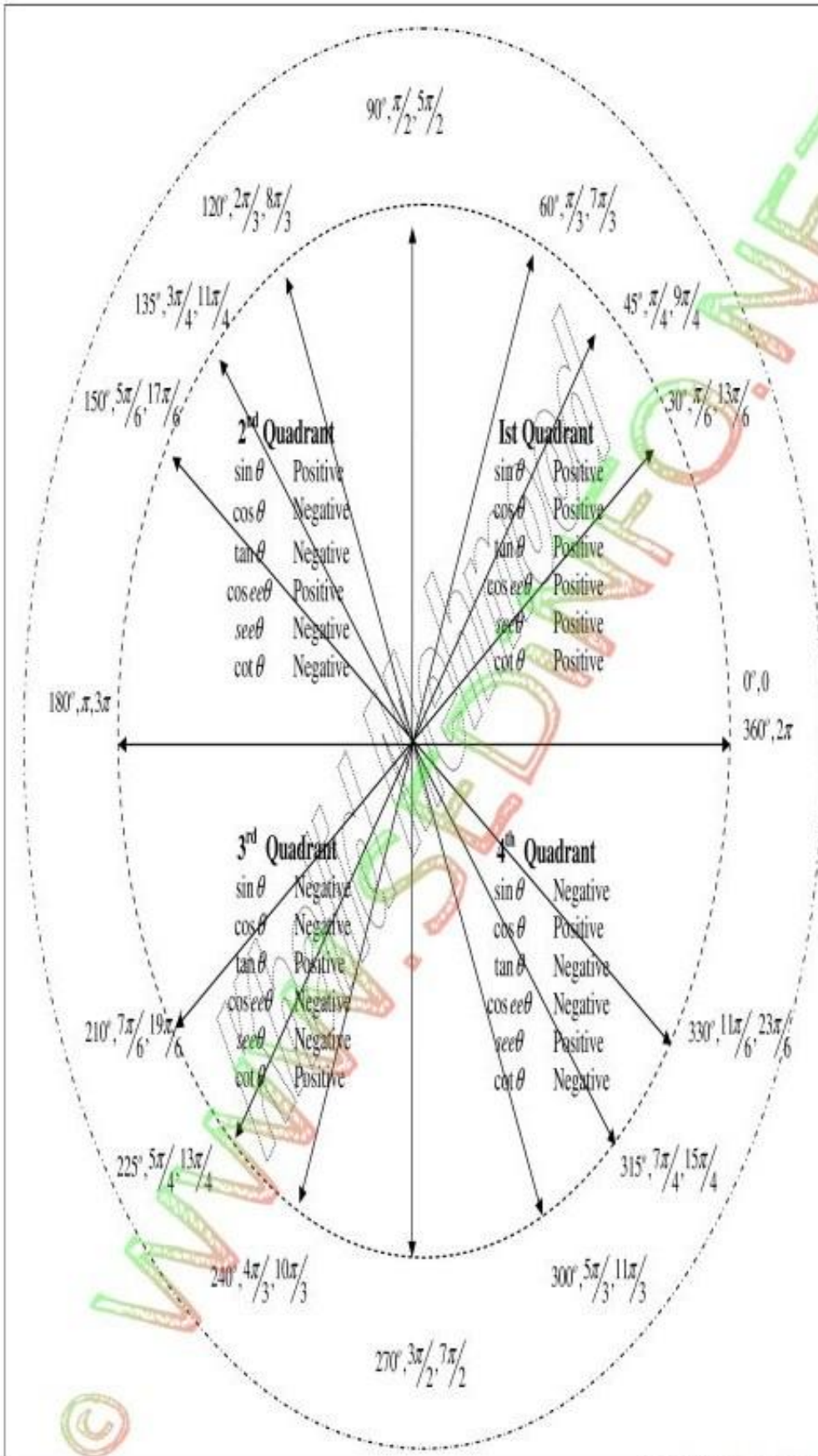
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Anti clock wise			Table for various Trigonometric Functions						Clock wise		
θ	1 st Round	2 nd Round	$\sin \theta$	$\cos \theta$	$\tan \theta$	$\operatorname{cosec} \theta$	$\sec \theta$	$\cot \theta$	θ	1 st Round	2 nd Round
0°	0	2 π	0	1	0	∞	1	∞	360°	2 π	4 π
30°	$\frac{\pi}{6}$	$\frac{13\pi}{6}$	$\frac{1}{2}=0.5$	$\frac{\sqrt{3}}{2}=0.866$	$\frac{1}{\sqrt{3}}=0.577$	2	$\frac{2}{\sqrt{3}}=1.155$	$\sqrt{3}=1.732$	330°	$\frac{11\pi}{6}$	$\frac{23\pi}{6}$
45°	$\frac{\pi}{4}$	$\frac{9\pi}{4}$	$\frac{1}{\sqrt{2}}=0.707$	$\frac{1}{\sqrt{2}}=0.707$	1	$\sqrt{2}=1.414$	$\sqrt{2}=1.414$	$\sqrt{2}=1.414$	315°	$\frac{7\pi}{4}$	$\frac{15\pi}{4}$
60°	$\frac{\pi}{3}$	$\frac{7\pi}{3}$	$\frac{\sqrt{3}}{2}=0.866$	$\frac{1}{2}=0.5$	$\sqrt{3}=1.732$	$\frac{2}{\sqrt{3}}=1.155$	2	$\frac{1}{\sqrt{3}}=0.577$	300°	$\frac{5\pi}{3}$	$\frac{11\pi}{3}$
90°	$\frac{\pi}{2}$	$\frac{5\pi}{2}$	1	0	∞	1	∞	0	270°	$\frac{3\pi}{2}$	$\frac{7\pi}{2}$
120°	$\frac{2\pi}{3}$	$\frac{8\pi}{3}$	$\frac{\sqrt{3}}{2}=0.866$	$-\frac{1}{2}=-0.5$	$-\sqrt{3}=-1.732$	$\frac{2}{\sqrt{3}}=1.155$	-2	$-\frac{1}{\sqrt{3}}=-0.577$	240°	$\frac{4\pi}{3}$	$\frac{10\pi}{3}$
135°	$\frac{3\pi}{4}$	$\frac{11\pi}{4}$	$\frac{1}{\sqrt{2}}=0.707$	$-\frac{1}{\sqrt{2}}=-0.707$	-1	$\sqrt{2}=1.414$	$-\sqrt{2}=-1.414$	-1	225°	$\frac{5\pi}{4}$	$\frac{13\pi}{4}$
150°	$\frac{5\pi}{6}$	$\frac{17\pi}{6}$	$\frac{1}{2}=0.5$	$-\frac{\sqrt{3}}{2}=-0.866$	$-\frac{1}{\sqrt{3}}=-0.577$	2	$-\frac{2}{\sqrt{3}}=-1.155$	$-\sqrt{3}=-1.732$	210°	$\frac{7\pi}{6}$	$\frac{19\pi}{6}$
180°	π	3 π	0	-1	0	∞	-1	∞	180°	π	3 π
210°	$\frac{7\pi}{6}$	$\frac{19\pi}{6}$	$-\frac{1}{2}=-0.5$	$-\frac{\sqrt{3}}{2}=-0.866$	$\frac{1}{\sqrt{3}}=0.577$	-2	$-\frac{2}{\sqrt{3}}=-1.155$	$\sqrt{3}=1.732$	150°	$\frac{5\pi}{6}$	$\frac{17\pi}{6}$
225°	$\frac{5\pi}{4}$	$\frac{13\pi}{4}$	$-\frac{1}{\sqrt{2}}=-0.707$	$-\frac{1}{\sqrt{2}}=-0.707$	1	$-\sqrt{2}=-1.414$	$-\sqrt{2}=-1.414$	1	135°	$\frac{3\pi}{4}$	$\frac{11\pi}{4}$
240°	$\frac{4\pi}{3}$	$\frac{10\pi}{3}$	$-\frac{\sqrt{3}}{2}=-0.866$	$-\frac{1}{2}=-0.5$	$\sqrt{3}=1.732$	$-\frac{2}{\sqrt{3}}=-1.155$	-2	$\frac{1}{\sqrt{3}}=0.577$	120°	$\frac{2\pi}{3}$	$\frac{8\pi}{3}$
270°	$\frac{3\pi}{2}$	$\frac{7\pi}{2}$	-1	0	∞	-1	∞	0	90°	$\frac{\pi}{2}$	$\frac{5\pi}{2}$
300°	$\frac{5\pi}{3}$	$\frac{11\pi}{3}$	$-\frac{\sqrt{3}}{2}=-0.866$	$\frac{1}{2}=0.5$	$-\sqrt{3}=-1.732$	$-\frac{2}{\sqrt{3}}=-1.155$	2	$-\sqrt{3}=-1.732$	60°	$\frac{\pi}{3}$	$\frac{7\pi}{3}$
315°	$\frac{7\pi}{4}$	$\frac{15\pi}{4}$	$-\frac{1}{\sqrt{2}}=-0.707$	$\frac{1}{\sqrt{2}}=0.707$	-1	$-\sqrt{2}=-1.414$	$\sqrt{2}=1.414$	-1	45°	$\frac{\pi}{4}$	$\frac{9\pi}{4}$
330°	$\frac{11\pi}{6}$	$\frac{23\pi}{6}$	$-\frac{1}{2}=-0.5$	$\frac{\sqrt{3}}{2}=0.866$	$-\frac{1}{\sqrt{3}}=-0.577$	-2	$\frac{2}{\sqrt{3}}=1.155$	$-\sqrt{3}=-1.732$	30°	$\frac{\pi}{6}$	$\frac{13\pi}{6}$
360°	2 π	4 π	0	1	0	∞	1	∞	0°	0	2 π





SOH \Rightarrow	$\sin \theta = \frac{\text{Opposite}}{\text{hypotenuse}}$
CAH \Rightarrow	$\cos \theta = \frac{\text{Adjacent}}{\text{hypotenuse}}$
TOA \Rightarrow	$\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$

If we have to find trigonometric ratio of $\sin 60$ then we will fold ring finger (finger of 60) and count how many finger are there left side of the folded finger that are three so $\sin 60 = \frac{\sqrt{3}}{2}$ in this way when we count how many fingers are right side of the folded finger that is only one finger so $\cos 60 = \frac{\sqrt{1}}{2} = \frac{1}{2}$

- $\sin^2 \theta + \cos^2 \theta = 1$
 - $\sin(-\theta) = -\sin \theta$
 - $1 + \tan^2 \theta = \sec^2 \theta$
 - $\cos(-\theta) = \cos \theta$
 - $1 + \cot^2 \theta = \csc^2 \theta$
 - $\tan(-\theta) = -\tan \theta$
-
- $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$
 - $\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$
 - $\tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta}$
 - $\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$
 - $\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$
 - $\tan(\alpha - \beta) = \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \tan \beta}$
-
- $\sin 2\theta = 2 \sin \theta \cos \theta$
 - $\cos 2\theta = \cos^2 \theta - \sin^2 \theta$
 - $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$
 - $\sin^2 \frac{\theta}{2} = \frac{1 - \cos \theta}{2}$
 - $\cos^2 \frac{\theta}{2} = \frac{1 + \cos \theta}{2}$
 - $\tan^2 \frac{\theta}{2} = \frac{1 - \cos \theta}{1 + \cos \theta}$
 - $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$
 - $\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$
 - $\tan 3\theta = \frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta}$
 - $\sin 2\theta = \frac{2 \tan \theta}{1 + \tan^2 \theta}$
 - $\cos 2\theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$
-
- $\sin(\alpha + \beta) + \sin(\alpha - \beta) = 2 \sin \alpha \cos \beta$
 - $\cos(\alpha + \beta) + \cos(\alpha - \beta) = 2 \cos \alpha \cos \beta$
 - $\sin \theta + \sin \phi = 2 \sin \frac{\theta + \phi}{2} \cos \frac{\theta - \phi}{2}$
 - $\cos \theta + \cos \phi = 2 \cos \frac{\theta + \phi}{2} \cos \frac{\theta - \phi}{2}$
 - $\sin^{-1} A + \sin^{-1} B = \sin^{-1} (A\sqrt{1-B^2} + B\sqrt{1-A^2})$
 - $\sin^{-1} A - \sin^{-1} B = \sin^{-1} (A\sqrt{1-B^2} - B\sqrt{1-A^2})$
 - $\cos^{-1} A + \cos^{-1} B = \cos^{-1} (AB - \sqrt{(1-A^2)(1-B^2)})$
 - $\cos^{-1} A - \cos^{-1} B = \cos^{-1} (AB + \sqrt{(1-A^2)(1-B^2)})$
 - $\sin(\alpha + \beta) - \sin(\alpha - \beta) = 2 \cos \alpha \sin \beta$
 - $\cos(\alpha + \beta) - \cos(\alpha - \beta) = -2 \sin \alpha \sin \beta$
 - $\sin \theta - \sin \phi = 2 \cos \frac{\theta + \phi}{2} \sin \frac{\theta - \phi}{2}$
 - $\cos \theta - \cos \phi = -2 \sin \frac{\theta + \phi}{2} \sin \frac{\theta - \phi}{2}$
 - $\tan^{-1} A + \tan^{-1} B = \tan^{-1} \frac{A+B}{1-AB}$
 - $\tan^{-1} A - \tan^{-1} B = \tan^{-1} \frac{A-B}{1+AB}$

Three Steps to solve $\sin\left(n \cdot \frac{\pi}{2} \pm \theta\right)$

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Step I: First check that n is even or odd

Step II: If n is even then the answer will be in \sin and if the n is odd then \sin will be converted to \cos and vice versa (i.e. \cos will be converted to \sin).

Step III: Now check in which quadrant $n \cdot \frac{\pi}{2} \pm \theta$ is lying if it is in *Ist* or *IInd* quadrant the answer will be positive as \sin is positive in these quadrants and if it is in the *IIIrd* or *IVth* quadrant the answer will be negative.

e.g. $\sin 667^\circ = \sin(7(90) + 37)$

Since $n = 7$ is odd so answer will be in \cos and 667 is in *IVth* quadrant and \sin is $-ive$ in *IVth* quadrant therefore answer will be in negative, i.e. $\sin 667^\circ = -\cos 37^\circ$

Similar technique is used for other trigonometric ratios, i.e. $\tan \Leftrightarrow \cot$ and $\sec \Leftrightarrow \csc$.